SHA1 is definitely more accurate than CRC32, just see the table below:

Number of 32-bit hash values	Number of 64-bit hash values	Number of 160-bit hash values	Odds of a hash collision	
77163	5.06 billion	1.42 × 10 ²⁴	1 in 2	
30084	1.97 billion	5.55 × 10 ²³	1 in 10	Odds of a full house in poker
9292	609 million	1.71 × 10 ²³	1 in 100	1 in 693 Odds of four-of-a-kind in poker 1 in 4164 Odds of being struck by lightning 1 in 576000
2932	192 million	5.41 × 10 ²²	1 in 1000 •	
927	60.7 million	1.71 × 10 ²²	1 in 10000	
294	19.2 million	5.41 × 10 ²¹	1 in 100000 .	
93	6.07 million	1.71 × 10 ²¹	1 in a million	Odds of winning a 6/49 lottery 1 in 13.9 million
30	1.92 million	5.41 × 10 ²⁰	1 in 10 million	Odds of dying in a shark attack
10	607401	1.71 × 10 ²⁰	1 in 100 million *	Odds of a meteor landing on your house 1 in 182 trillion
	192077	5.41 × 10 ¹⁹	1 in a billion	
	60740	1.71 × 10 19	1 in 10 billion	
	19208	5.41 × 10 ¹⁸	1 in 100 billion	
	6074	1.71 × 10 ¹⁸	1 in a trillion	
	1921	5.41 × 10 ¹⁷	1 in 10 trillion	
	608	1.71 × 10 ¹⁷	1 in 100 trillion	
	193	5.41 × 10 ¹⁶	1 in 10 ¹⁵	
	61	1.71 × 10 ¹⁶	1 in 10 ¹⁶	
	20	5.41 × 10 15	1 in 10 ¹⁷	
	7	1.71 × 10 15	1 in 10 ¹⁸	

(Image taken from a great

article: Hash Collision Probabilities).

CRC32 is 32-bit, SHA1 is 160-bit. So if you check 100 files, there will be approx. 1 in a million chance that for two of them CRC32 hashes will collide and report files as duplicates when they are not. On the other hand, with SHA1 the chance will be 9 orders of magnitude less: approx. 1 in 10^{15} .

However SHA1 is also more complex to compute, whereas CRC32 is rather simple. It might make sense to employ both: CRC32 first, and then SHA1 to make sure that files with same CRC32 hashes are indeed duplicates of each other.

But if you are writing an utility that will find and delete duplicate files, think if you can afford even such miniscule probability of a false positive. Probably you'll have to do a bit-by-bit comparison of the files as the final check.

Update: also consider that for large files, more efficient method is to not use hashes of the whole file, but read and hash files by blocks. This way, you'll be able to quit checking as soon as you hit first different block.